

# The Condensate and Its Shadows

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### Gravity, Information, the Arrow of Time, and Complexity as Regimes of a Single Ginzburg-Landau Order Parameter

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#### Abstract

A single complex scalar order parameter  $W_0$ , governed by the GL action  $S[W_0] = \int (|dW_0|^2 + a_0|W_0|^2 + (b_0/2)|W_0|^4)$   $d\mu$ , generates as limiting regimes: (i) gravity as the mean-field geometry of the condensed phase; (ii) black-hole information preservation through unitarity of the GL partition function and replica wormhole saddles; (iii) the arrow of time as monotonically increasing condensate complexity, supported by the Komargodski-Schwimmer a-theorem; (iv)  $P \neq NP$  as a structural consequence of the topological irreducibility of the pre-geometric phase.  $W_0$  is identified with the Will Field of the RTSG framework.

#### 1. Setup

The companion paper (RTSG-2026-001) established that gravity is a GL condensation phenomenon – spacetime is the condensed phase of  $W_0$ , horizons are phase boundaries, and surface gravity  $\kappa$  is the logarithmic rate of the condensate at the boundary:

$$\kappa = -(d/du) \ln|W_0| \quad \text{at the horizon}$$

#### 2. The Kinematic Clock

The GL condensate at the phase boundary has a natural relaxation timescale:

$$t_{\text{kin}} = S_{\text{Wald}} / \kappa$$

For Schwarzschild:  $t_{\text{kin}}$  recovers the scrambling time  $\sim 8\pi M^{2G}$ . For de Sitter:  $t_{\text{kin}}$  recovers the Poincare recurrence time  $\sim \pi/(GH_3)$ . Both follow from the condensate clock without additional assumptions.

#### 3. Information Preservation

The information paradox dissolves when information loss is recognized as a phase transition, not a destruction event.

**Correct mechanism:** Unitarity of the full GL partition function  $Z = \int DW_0 \exp(-S[W_0])$ . Replica wormhole saddles [Penington et al. 2019] restore the Page curve at  $t > t_{\text{Page}}$ . The  $U(1)$  symmetry of the GL action provides structural conservation of winding numbers (topological vortices), but information preservation requires the full unitary path integral.

**Correction note:**  $U(1)$  conservation preserves one Noether charge, not the full quantum state. Earlier versions of this claim were a category error; this is the corrected formulation.

## 4. Arrow of Time

The KS a-theorem [Komargodski-Schwimmer 2011] guarantees monotone RG flow from UV ( $c=1, T=T_c$ ) to IR ( $c=0, T>0$ ). Active degrees of freedom decrease monotonically – the condensate becomes more ordered.

**Status:**  $dS_{\text{ent}}/dt \geq 0$  during Big Bang condensation is a well-motivated conjecture supported by exact results in 1+1D analogues [Calabrese-Cardy 2005] and RG monotonicity. Full proof requires the 3+1D quantum quench calculation – currently open.

**Correction note:** An earlier version used strong subadditivity (SSA) to prove this. SSA gives  $S(A \cup B) \leq S(A) + S(B)$  – an upper bound, not a lower bound. The SSA argument was direction-reversed and has been replaced.

**Physical meaning:** The Second Law is not a fundamental postulate. It is the statement that the universe is still in the middle of its Big Bang phase transition. Entropy increases because condensate complexity increases.

## 5. Black Hole as Local Phase Inversion

Black hole evaporation is a localized phase inversion, not a time-reversal or exact symmetry. The tidal Weyl curvature drives the effective  $a_0^{\text{eff}}(r)$  toward positive values inside the horizon, causing  $W_0 \rightarrow 0$  locally. This traverses the same Mexican-hat potential in the opposite direction from the Big Bang condensation – not related by a symmetry.

**Correction note:** Earlier versions called this an “exact symmetry under  $a_0 \rightarrow -a_0$ .” This is wrong.  $a_0 \rightarrow -a_0$  is a parameter change that drives a phase transition, not a symmetry of the GL action.

## 6. $P \neq NP$ from Phase Topology

NP-complete problems require traversing the pre-geometric (uncondensed) phase – the full configuration space of  $W_0$ . P problems are solvable within the condensed phase. The kinematic clock  $t_{\text{kin}} = S/\kappa$  gives the time to process one bit of the phase boundary. Traversing the full pre-geometric space requires exponentially many such bits.

**Status:** Structural argument, not a formal complexity-theoretic proof. Requires mapping logical gates to GL topological invariants.

## 7. The Complexity Gradient

One field, four regimes:

- Gravity: condensate at minimum complexity ( $\min |dW_0|$ )
- Electromagnetism, Yang-Mills: intermediate complexity
- Matter, chemistry, biology: high complexity
- Consciousness, computation: maximum local complexity

## 8. RTSG Identification

$W_0 = W_{\text{RTSG}}$  (the RTSG Will Field).

Three Spaces = three phases of the condensate: - Potentiality Space = uncondensed phase ( $W_0 = 0$ ) - Context Space = phase boundary (critical surface) - Actuality Space = condensed phase ( $|W_0| = v_0$ )

The complexification functor  $C = \text{GL gradient flow}$ . The ContextualObstruction = topological barrier of the phase transition.

## References

[1] J.-P. Niko, “Gravity as Geometric Condensation,” RTSG-2026-001 (2026). [2] G. Penington et al., “Replica Wormholes,” arXiv:1911.11977 (2019). [3] Z. Komargodski and A. Schwimmer, JHEP 12, 099 (2011). [4] P. Calabrese and J. Cardy, J. Stat. Mech. P04010 (2005). [5] A. Almheiri et al., Rev. Mod. Phys. 93, 035002 (2021).